

1. Study Section 8.4.
2. Do Exercise 8.5.
These are all one-step proofs!
3. Prove (8.23b), Split off term.
4. Extra credit. Not required.
The proof of (8.23a) Split off term uses the fact that

$$0 \leq i < n + 1 \equiv 0 \leq i < n \vee i = n$$

under the assumption that $n: \mathbb{N}$, that is, $0 \leq n$. Give a detailed proof of this fact by filling in the steps of the formal proof below from the hints.

$$\begin{aligned}
 & 0 \leq i < n + 1 \\
 = & \langle \text{Remove the conjunctive abbreviation} \rangle \\
 \\
 = & \langle i < n + 1 \equiv i < n \vee i = n \rangle \\
 \\
 = & \langle (3.46) \wedge \text{ distributes over } \vee \rangle \\
 \\
 = & \langle (3.84a) \text{ Substitution} \rangle \\
 \\
 = & \langle \text{Assumption } 0 \leq n \rangle \\
 \\
 = & \langle (3.39) \text{ Identity of } \wedge \rangle \\
 \\
 = & \langle \text{Reintroduce conjunctive abbreviation} \rangle \\
 & 0 \leq i < n \vee i = n
 \end{aligned}$$