

There are five techniques for proving an implication:

- Equivalence to a previous theorem
- Antecedent implies consequent
- Consequent follows from antecedent
- Deduction – assume the conjuncts of the antecedent
- Contrapositive

The following table summarizes the first four of these techniques to prove  $P_1 \wedge P_2 \Rightarrow Q$ .

Equivalence to a previous theorem	Antecedent implies consequent	Consequent follows from antecedent	Deduction – assume the conjuncts of the antecedent
Start with entire theorem	Start with antecedent	Start with consequent	Start with consequent
$P_1 \wedge P_2 \Rightarrow Q$ $= \langle \dots \rangle$ $\dots$ $= \langle \dots \rangle$ $\dots$ $= \langle \dots \rangle$ $\dots$ $= \langle \dots \rangle$ <p>Previous theorem or true //</p> <p>all =</p>	$P_1 \wedge P_2$ $= \langle \dots \rangle$ $\dots$ $\Rightarrow \langle \dots \rangle$ $\dots$ $= \langle \dots \rangle$ $\dots$ $\Rightarrow \langle \dots \rangle$ <p><math>Q</math> //</p> <p>= or <math>\Rightarrow</math></p>	$Q$ $= \langle \dots \rangle$ $\dots$ $\Leftarrow \langle \dots \rangle$ $\dots$ $\Leftarrow \langle \dots \rangle$ $\dots$ $= \langle \dots \rangle$ <p><math>P_1 \wedge P_2</math> //</p> <p>= or <math>\Leftarrow</math></p>	$Q$ $= \langle \text{Assume conjunct } P_1 \rangle$ $\dots$ $= \langle \dots \rangle$ $\dots$ $= \langle \text{Assume conjunct } P_2 \rangle$ $\dots$ $= \langle \dots \rangle$ <p>Previous theorem or true //</p> <p>all =</p>

The contrapositive of

$$P_1 \wedge P_2 \Rightarrow Q$$

is

$$\neg Q \Rightarrow \neg(P_1 \wedge P_2)$$

which can be proved using any of the above four proof techniques with  $\neg Q$  as the antecedent and  $\neg(P_1 \wedge P_2)$  as the consequent.